

## MILLIMETER- AND SUBMILLIMETER-WAVE DETECTION BY PARAMAGNETIC MATERIALS\*

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INTRODUCTION

Due to a lack of powerful signal sources in the millimeter- and submillimeter-wavelength range, a sensitive detector is an essential requirement for work in this frequency band. Adaptations of microwave and optical devices to this wavelength region have many limitations. One means of circumventing the problems associated with operation in this region is to convert the short wavelength radiation to lower frequencies where low noise detection techniques are available.<sup>1-4</sup> This paper describes the theoretical and experimental evaluation of a downconverter which utilizes paramagnetic materials. Using materials with appropriate zero field splittings this device should be operable over the millimeter- through far-infrared-wavelength range.

DOWNCONVERTER OPERATION

The paramagnetic downconverter is essentially a frequency converter which transfers the information on the millimeter-wave signal to a microwave signal. An energy-level diagram appropriate for the operation of this device is shown in Fig. 1. When a millimeter-wave signal of frequency  $\nu_{13}$  is incident, the population of level 3 will be increased and that of level 1 will be decreased. Under ideal conditions, the extra electrons in level 3 will relax to level 2 thereby increasing its population. A microwave signal of frequency  $\nu_{12}$  can detect this change in population. Therefore the information on the millimeter-wave signal is now superimposed on the microwave signal. Using a low noise receiver at the microwave frequency, sensitive detection of the millimeter-wave signal can be achieved.

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## NOTES

### CONVERSION LOSS

The conversion loss is an important parameter in the operation of any frequency translation device. The rate equations<sup>5</sup> can be used to estimate the conversion loss expected in the paramagnetic downconverter. These equations describe the response of the level populations to thermal relaxation and external excitation processes.

The time dependence of the  $i$ th level population is given by the equation

$$\frac{dn_i}{dt} = \sum_{j=1}^3 [-(\omega_{ij} + W_{ij})n_i + (\omega_{ji} + W_{ji})n_j] , \quad (1)$$

where  $n_i$  = the population of level  $i$ ,

$\omega_{ij}$  = the thermal relaxation rate from level  $i$  to level  $j$  and

$W_{ij}$  = the stimulated transition rate from level  $i$  to level  $j$ .

The solution of these equations for small  $W_{13}$  shows that

$$n_1 - n_2 \approx \frac{(n_1 - n_2)^0 - T_{13} W_{13}}{1 + T_{12} W_{12}} . \quad (2)$$

Here  $T_{12}$  and  $T_{13}$  are relaxation times related to the  $\omega_{ij}$  terms.

The power absorbed at  $\nu_{12}$  is

$$P_{12} = h\nu_{12} (n_1 - n_2) W_{12} , \quad (3)$$

where  $h$  is Planck's constant. Thus the decrease in power absorption  $\Delta P_{12}$  due to the presence of the millimeter-wave signal is

$$\Delta P_{12} = -\frac{h\nu_{12} T_{13} W_{13}}{1 + T_{12} W_{12}} . \quad (4)$$

Therefore the general form for this equation can be written in the form

$$\Delta P_{12} = \frac{LP_{mm} P_{12}^i}{1 + P_{12}^i / P_{sat}^i} , \quad (5)$$

where  $P_{mm}$  = the millimeter-wave power level,  
 $P_{12}^i$  = the incident power at  $\nu_{12}$ ,  
 $P_{sat}^i$  = the saturation input power at  $\nu_{12}$  and  
 $L$  = a constant.

In this case the downconversion loss is

$$L_{dc} = \frac{1 + P_{12}^i / P_{sat}^i}{LP_{12}^i} . \quad (6)$$

#### NOISE SOURCES

There are three main sources of noise in this device. First, amplitude and frequency fluctuations in the local oscillator will appear as amplitude fluctuations in the microwave output. Second, the microwave frequency transition has an equivalent noise temperature. This temperature will increase as the local oscillator power level increases since the level populations will tend to be equalized thereby increasing their apparent noise temperature. Finally, the noise figure of the following amplifier must be accounted for in determining the minimum detectable power for the downconverter.

In the downconverter, the changes in power absorption at the microwave frequency are determined by monitoring the power reflected by the device. Since the millimeter-wave power causes small changes in the microwave power level, the detection problem is one of determining small changes in a relatively large power level. In this situation the smallest observable change in power is<sup>6</sup>

$$\Delta P_{12} = 2 \sqrt{P_n P_{12}^0} , \quad (7)$$

where  $P_n$  is the noise power at the device output as determined by the three sources above and  $P_{12}^0$  is the microwave power level at the output terminal.

Combining Eqs. 6 and 7 and optimizing with respect to  $P_{12}^i$  shows that

$$(P_{mm})_{min} = \frac{4 \sqrt{P_n P_{12}^0}}{LP_{sat}^i} . \quad (8)$$

If the downconverter and local oscillator do not contribute significantly to  $P_n$ , then

$$(P_{mm})_{\min} = \frac{4 \sqrt{F_A k T B P^0}}{L P_{sat}^i} \quad , \quad (9)$$

where  $F_A$  = the following amplifier noise figure and

$B$  = the following amplifier bandwidth.

In Fig. 2 the values of  $(P_{mm})_{\min}$  and  $(NEP)_{mm}$  ( $B = 1$  Hz) are tabulated for liquid nitrogen and liquid helium operation. These calculations assume reasonable operating parameters for the downconverter and optimized external circuit. Preliminary measurements on a nonoptimum external circuit tend to confirm the theoretical predictions.

#### EXPERIMENTAL RESULTS

An experimental model of the device described above has been built and operated successfully at 4°K and 77°K. In these experiments input frequencies were in the 35 to 60 GHz range so that an accurate evaluation of the device characteristics could be made. The microwave output frequency in these experiments was about .9 GHz. Figure 3 shows the energy level diagram for one operating point. Figures 4 and 5 are experimental results of some liquid nitrogen temperature measurements at this operating point. Figure 6 shows the input and output signals of the downconverter. Further work is underway to evaluate the response time and minimum detectable power for this device.

#### CONCLUSIONS

The feasibility of operating a downconverter as described above has been demonstrated. It is felt that the initial results warrant further investigations especially with input frequencies above 100 GHz where sensitive detectors are not readily available.

LIST OF REFERENCES

1. Basov, N. G. and Karlov, N. V., "On a Wideband Radiometer with Quantum Spectrum Converter," Radio Eng. Electron. (USSR), vol. 5, No. 4, pp. 204-206; April, 1960.
2. Shimoda, K., "Three-Level Maser Detector for Ultra-Microwaves," Jour. Phys. Soc. Japan, vol. 14, No. 7, p. 966; July, 1959.
3. Haddad, G. I. and Krumm, C. F., "Paramagnetic Materials for Millimeter- and Submillimeter-Wave Detection," Presented at Boulder Millimeter and Far Infrared Conference, Estes Park, Colorado; August, 1965.
4. Bloembergen, N., "Solid State Infrared Quantum Counter," Phys. Rev. Letters, vol. 2, pp. 84-85; February 1, 1959.
5. Seigman, A. E., Microwave Solid State Masers, McGraw Hill Co., Inc., New York; 1964.
6. Townes, C. and Geschwind, S., "Limiting Sensitivity of a Microwave Spectrometer," Jour. Appl. Phys., vol. 19, No. 8, pp. 795-796; August, 1948.

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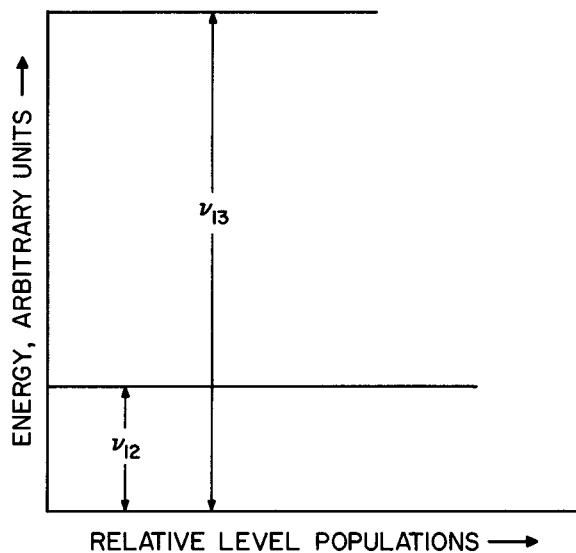


FIG. 1 ENERGY LEVELS SUITABLE FOR PARAMAGNETIC DOWNCONVERTER OPERATION.

$T_D$	77°K	4°K
L	10	1000
$P_{sat}^i$	2.5 mW	25 $\mu$ W
$P_{12}^o$	2.5 nW	25 pW
$F_A$	4	4
B	1 MHz	1 MHz
T	290°K	290°K
$(P_{mm})_{min}$	$5 \cdot 10^{-11}$ W	$1.6 \cdot 10^{-13}$ W
NEP <sub>mm</sub>	$5 \cdot 10^{-14}$ W	$1.6 \cdot 10^{-16}$ W

FIG. 2 DOWNCONVERTER MINIMUM DETECTABLE POWER.

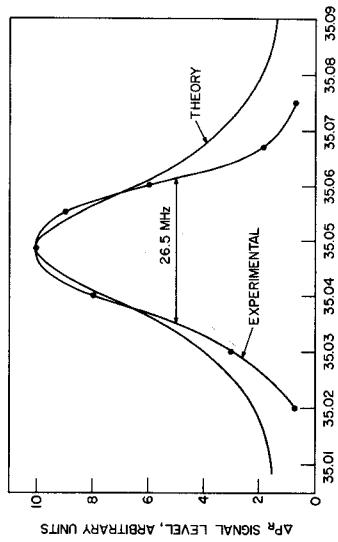


FIG. 3 ENERGY LEVEL SEPARATION, GHz VS. MAGNETIC FIELD, kg FOR DOWNCONVERSION FROM 35 GHz TO 9 GHz.

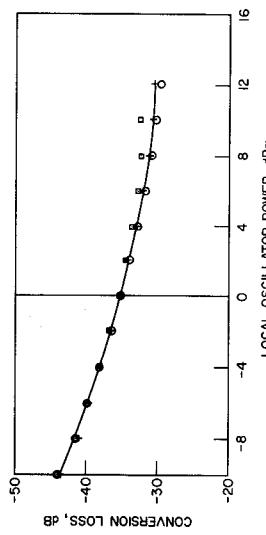
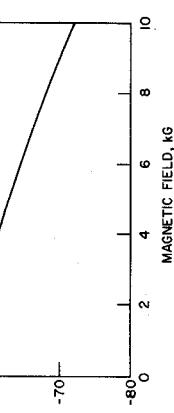


FIG. 4 INPUT RESPONSE OF DOWNCONVERTER.

FIG. 5 DOWNCONVERTER OVERALL CONVERSION LOSS (LINE AND MISMATCH LOSSES = 8.3 dB).



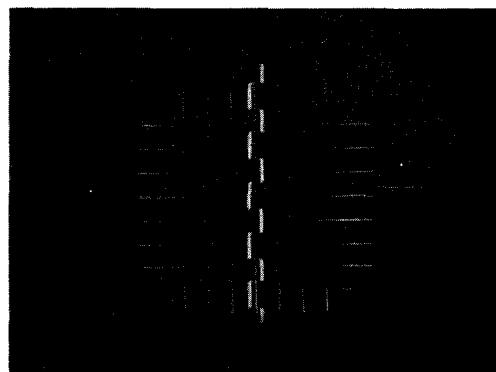
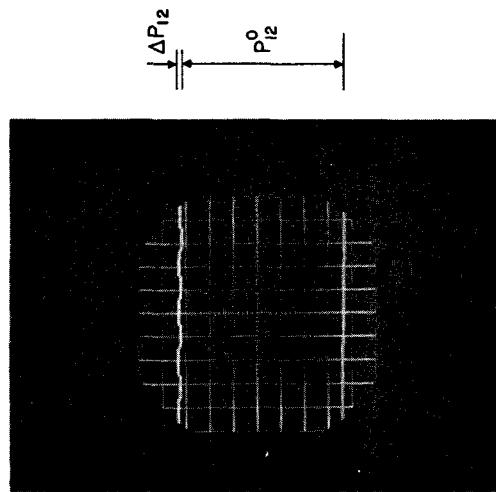


FIG. 6 INPUT AND OUTPUT SIGNALS FROM DOWNCONVERTER.